Measurement of the near-threshold $e^+e^- \to D\bar{D}$ cross section using initial-state radiation


(The Belle Collaboration)

1Budker Institute of Nuclear Physics, Novosibirsk
2Chiba University, Chiba
3University of Cincinnati, Cincinnati, Ohio 45221
4Justus-Liebig-Universität Gießen, Gießen
5The Graduate University for Advanced Studies, Hayama
6Gyeongsang National University, Chinju
7Hanyang University, Seoul
8University of Hawaii, Honolulu, Hawaii 96822
9High Energy Accelerator Research Organization (KEK), Tsukuba
10University of Illinois at Urbana-Champaign, Urbana, Illinois 61801
11Institute of High Energy Physics, Chinese Academy of Sciences, Beijing
12Institute of High Energy Physics, Vienna
13Institute of High Energy Physics, Protvino
14Institute for Theoretical and Experimental Physics, Moscow
15J. Stefan Institute, Ljubljana
16Kyungpook National University, Taegu
17École Polytechnique Fédérale de Lausanne (EPFL), Lausanne
18University of Ljubljana, Ljubljana
19University of Maribor, Maribor
20University of Melbourne, School of Physics, Victoria 3010
21Nagoya University, Nagoya
22Nara Women’s University, Nara
23National Central University, Chung-li
24National United University, Miaoli Li
25Department of Physics, National Taiwan University, Taipei
26H. Niewodniczanski Institute of Nuclear Physics, Krakow
27Nippon Dental University, Niigata
28Niigata University, Niigata
29University of Nova Gorica, Nova Gorica
30Osaka City University, Osaka
31Osaka City University, Osaka
32Panjab University, Chandigarh
33RIKEN BNL Research Center, Upton, New York 11973
34Saga University, Saga
35University of Science and Technology of China, Hefei
36
We report measurements of the exclusive cross section for $e^+e^-$ → $D\bar{D}$, where $D = D^0$ or $D^+$, in the center-of-mass energy range from the $D\bar{D}$ threshold to 5 GeV with initial-state radiation. The analysis is based on a data sample collected with the Belle detector with an integrated luminosity of 673 fb$^{-1}$.

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The total cross section for hadron production in $e^+e^-$ annihilation in the $\sqrt{s}$ region above the open-charm threshold was measured precisely by the Crystal Ball [1] and BES [2] Collaborations. However, the parameters of the old was measured precisely by the Crystal Ball [1] and $\gamma_{ISR}$ in the detector acceptance in which case the polar angle for the $D\bar{D}$ combination in the c.m. frame is required to be $|\cos(\theta_{D\bar{D}})| > 0.9$; (2) the $\gamma_{ISR}$ is within the detector acceptance ($|\cos(\theta_{D\bar{D}})| < 0.9$), in this case the $\gamma_{ISR}$ is required to be detected and the mass of the $D\bar{D}\gamma_{ISR}$ combination is required to be greater than $E_{c.m} - 0.58$ GeV/c$^2$. To suppress background from $e^+e^- → D\bar{D}(\pi)\pi\gamma_{ISR}$ processes we exclude events that contain additional charged tracks that are not used in the $D$ or $D$ reconstruction.

We ensure that all charged tracks originate from the interaction point (IP) with the requirements $dr < 2$ cm and $|dz| < 4$ cm, where $dr$ and $|dz|$ are the impact parameters perpendicular to and along the beam direction with respect to the IP. Charged kaons are required to have a ratio of particle identification likelihoods, $P_K = \mathcal{L}_K/(\mathcal{L}_K + \mathcal{L}_\pi)$ [15], larger than 0.6. No identification requirements are applied for pion candidates. $K_S^0$ candidates are reconstructed from $\pi^+\pi^-$ pairs with an invariant mass within 10 MeV/c$^2$ of the nominal $K_S^0$ mass. The distance between the two pion tracks at the $K_S^0$ vertex must be less than 1 cm, the transverse flight distance from the interaction point is required to be greater than 0.1 cm, and the angle between the $K_S^0$ momentum direction and the flight direction in the $x - y$ plane should be smaller than 0.1 rad. The pion pair candidates are refit to the $K_S^0$ mass. Photons are reconstructed in the electromagnetic calorimeter as showers with energies greater than 50 MeV that are not associated with charged tracks. Pairs of photons are combined to form $\pi^0$ candidates. If the mass of a $\gamma\gamma$ pair lies within 15 MeV/c$^2$...
of the nominal $\pi^0$ mass, the pair is fit with a $\pi^0$ mass constraint and considered as a $\pi^0$ candidate. $D^0$ candidates [16] are reconstructed using five decay modes: $K^+\pi^-$, $K^-\pi^+$, $K^-\pi^+\pi^+$, $K_S^0\pi^+\pi^-$ and $K^-\pi^+\pi^0$. $D^+$ candidates are reconstructed using the decay modes $K_S^0\pi^+$ and $K^-\pi^+\pi^+$. A $\pm 15$ MeV$/c^2$ mass window is used for all modes except for $K^-\pi^-\pi^+\pi^+$, where a $\pm 10$ MeV$/c^2$ requirement is applied ($\sim 2.5\sigma$ in each case). To improve the momentum resolution of $D$ meson candidates, final tracks are fitted to a common vertex and a $D^0$ or $D^+$ mass constraint is applied. The $D$ candidates from a sideband region are reﬁtted to the mass, corresponding to the center of the sideband region with the same width as the signal window.

The distribution of $M_{rec}^2(D\bar{D})$ after all the requirements is shown in Fig. 1(a). A clear peak corresponding to the $e^+e^-\rightarrow D\bar{D}\gamma_{ISR}$ process is evident around zero. The shoulder at positive values is due to $e^+e^-\rightarrow D^{(*)}\bar{D}(n)\pi^0\gamma_{ISR}$ events. To suppress the tail of such events we deﬁne a signal region by the requirement: $|M_{rec}^2(D\bar{D})|<0.7$ (GeV$/c^2$)$^2$. The polar angle distribution for $D\bar{D}$ after the requirements on $M_{rec}^2(D\bar{D})$ is shown in Fig. 1(c). The sharp peaking at $\pm 1$ is characteristic of ISR production and agrees with the Monte Carlo (MC) simulation. The mass distribution of the $D\bar{D}\gamma_{ISR}$ combinations where the $\gamma_{ISR}$ is detected is shown in Fig. 1(b) after all the selection requirements. It peaks at the $E_{c.m.}$ . The asymmetric shape of the $M_{D\bar{D}}\gamma_{ISR}$ distribution is due to higher-order ISR processes.

The $M_{D\bar{D}}$ and $M_{D^+D^-}$ spectra obtained after all the requirements are shown in Fig. 2.

![FIG. 1](color online). The observed distributions of (a) $M_{rec}^2(D\bar{D})$; (b) $M(DD\gamma_{ISR})$ and (c) $D\bar{D}$ polar angles. Histograms show the normalized contributions from $M_D$ and $M_{D^0}$ sidebands. The selected signal windows are illustrated by vertical lines.

![FIG. 2](The mass spectra of $D\bar{D}$ combinations (points with error bars): (a) $D^0\bar{D}^0$; (b) $D^+D^-$. The total contribution from combinatorial background (1–2) is shown as the hatched histogram, the contribution from background (4) is shown as the (barely visible) solid histogram.

The following sources of background are considered:

1. combinatorial $D(D)$ mesons combined with a real $D(D)$ coming from the signal or other processes;
2. both $D$ and $\bar{D}$ are combinatorial;
3. reflection from the processes $e^+e^-\rightarrow D\bar{D}\pi_0$ mass $\gamma_{ISR}$ and $e^+e^-\rightarrow D\bar{D}\gamma_{ISR}$, followed by $D^0\rightarrow D\pi_0$ mass, with an extra $\pi_0$ mass in the final state;
4. reflection from the process $e^+e^-\rightarrow D\bar{D}^*\gamma_{ISR}$, followed by $D^0\rightarrow D\bar{D}\gamma$, with an extra soft $\gamma$ in the final state;
5. a contribution from $e^+e^-\rightarrow D\bar{D}\pi_0$ when an energetic $\pi_0$ is misidentiﬁed as a single $\gamma_{ISR}$.

The contribution from background (1) is extracted using $M_D$ and $M_{D^0}$ sidebands that are 4 times as large as the signal region. These sidebands are shifted by 30 MeV$/c^2$ (20 MeV$/c^2$ for the $D^0\rightarrow K^-\pi^-\pi^+\pi^+$ mode) from the signal region to avoid signal over-subtraction. Background (2) is present in both the $M_D$ and $M_{D^0}$ sidebands and is, thus, subtracted twice. To account for this over-subtraction we use a 2-dimensional sideband region, where events are selected from both the $M_D$ and $M_{D^0}$ sidebands. The total contribution of the combinatorial backgrounds (1–2) is shown in Fig. 2 as a hatched histogram. Backgrounds (3–4) are suppressed by the tight requirement on $M_{rec}^2(D\bar{D})$. The remaining contribution from background (3) is estimated directly from the data by applying a similar full reconstruction method to the isospin-conjugate process $e^+e^-\rightarrow D\bar{D}^*\pi_0$ mass $\gamma_{ISR}$. Here the requirement on absence of additional charged tracks in the event is relaxed. Since there is a charge imbalance in the $D^0\bar{D}^-$ final state, only events with an extra missing $\pi_0$ mass can contribute to the $M_{rec}^2(D\bar{D})$ signal window. To extract the level of back-
ground (3), the $D^0 D^-$ mass spectrum is rescaled according to the ratio of $D^0$ and $D^-$ reconstruction efficiencies and an isospin factor of $1/2$. When this is done, the contribution from background (3) is found to be negligibly small. Uncertainties in this estimate are included in the systematic error. Background (4) contributes only to the $D^0 \bar{D}^0$ final state. It is estimated using an MC simulation of $e^+ e^- \rightarrow D^0 \bar{D}^0 \gamma_{\text{ISR}}$, followed by $\bar{D}^0 \rightarrow D^0 \gamma$. To reproduce the shape of the $D^0 \bar{D}^0$ mass distribution we use the $D^\pm D^\mp$ cross section measured in our previous study [7]. The contribution from background (4) is found to be small (shown in Fig. 2(a) as a solid histogram) and is subtracted from the $D^0 \bar{D}^0$ mass spectrum. Uncertainties in this estimate are included in the systematic error. The contribution from background (5), determined from reconstructed $e^+ e^- \rightarrow D\bar{D} \pi^0$ events in the data, is found to be negligibly small and taken into account in the systematic error.

The $e^+ e^- \rightarrow D\bar{D}$ cross sections are extracted from the $D^0 \bar{D}^0$ and $D^+ D^-$ mass distributions [17]

$$\sigma(e^+ e^- \rightarrow D\bar{D}) = \frac{dN/dm}{\eta_{\text{tot}} dL/dm},$$

where $m = M_{D\bar{D}}$, $dN/dm$ is the obtained mass spectrum, while $\eta_{\text{tot}}$ is the total efficiency. The factor $dL/dm$ is the differential ISR luminosity

$$dL/dm = \frac{C}{\pi x^2 (2 - 2x + x^2)} \ln \frac{1 + C}{1 - C} - x^2 C \frac{2m L}{E_{\text{c.m.}}}.$$

where $x = 1 - m^2 / E_{\text{c.m.}}^2$, $L$ is the total integrated luminosity and $C = \cos \theta_0$, where $\theta_0$ defines the polar angle range for the $\gamma_{\text{ISR}}$ in the $e^+ e^-$ c.m. frame: $\theta_0 < \gamma_{\text{ISR}} < 180^\circ - \theta_0$. The total efficiency determined by MC simulation grows linearly with $M_{D\bar{D}}$ from 0.95% near threshold to 0.46% at 5 GeV/$c^2$ for the $D^0 \bar{D}^0$ and from 0.038% to 0.17% for the $D^+ D^-$ mode. The resulting $e^+ e^- \rightarrow D^0 \bar{D}^0$, $e^+ e^- \rightarrow D^+ D^-$ and $e^+ e^- \rightarrow D\bar{D}$ exclusive cross sections, averaged over the bin width, are shown in Fig. 3 with statistical uncertainties only.

Since the bin width in the cross section distributions is much larger than the resolution (which is $\sim 3$ MeV/$c^2$ at threshold and $\sim 5$ MeV/$c^2$ at $M_{D\bar{D}} \sim 5$ GeV/$c^2$), no correction for resolution is applied.

We calculate the cross section ratio $\sigma(e^+ e^- \rightarrow D^+ D^-)/\sigma(e^+ e^- \rightarrow D^0 \bar{D}^0)$ for the $M_{D\bar{D}}$ bin (3.76–3.78) GeV/$c^2$ corresponding to $M_{D\bar{D}} = M_{D(3770)}$ to be $(0.72 \pm 0.16 \pm 0.06)$. This value is in agreement within errors with the CLEO Collaboration [18] and BES [19] measurements. The ratio $\sigma(e^+ e^- \rightarrow D^+ D^-)/\sigma(e^+ e^- \rightarrow D^0 \bar{D}^0)$ integrated over the $M_{D\bar{D}}$ range from 3.8 to 5.8 GeV/$c^2$ is found to be $(1.15 \pm 0.13 \pm 0.10)$ and is consistent with unity.

The systematic errors for the $\sigma(e^+ e^- \rightarrow D\bar{D})$ measurements are summarized in Table I.

### Table I. Contributions to the systematic error in the cross sections, [%].

<table>
<thead>
<tr>
<th>Source</th>
<th>$D^0 \bar{D}^0$</th>
<th>$D^+ D^-$</th>
<th>$D\bar{D}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Background subtraction</td>
<td>±4</td>
<td>±3</td>
<td>±3</td>
</tr>
<tr>
<td>Reconstruction</td>
<td>±7</td>
<td>±6</td>
<td>±7</td>
</tr>
<tr>
<td>Cross section calculation</td>
<td>±5</td>
<td>±5</td>
<td>±5</td>
</tr>
<tr>
<td>$B(D)$</td>
<td>±4</td>
<td>±6</td>
<td>±5</td>
</tr>
<tr>
<td>Kaon identification</td>
<td>±2</td>
<td>±2</td>
<td>±2</td>
</tr>
<tr>
<td>Total</td>
<td>±10</td>
<td>±10</td>
<td>±10</td>
</tr>
</tbody>
</table>

The systematic errors associated with the background (1–2) subtraction are estimated to be 2% due to the uncertainty in the scaling factors for the sideband subtractions. This systematic error is estimated using fits to the $M_D$ and $M_{D\bar{D}}$ distributions with different signal and background parametrizations. Uncertainties in backgrounds (3–5) are conservatively estimated to be smaller than 2% of the signal in the case of $D^0 \bar{D}^0$; these two sources are added linearily to give 4% in total. In the $D^+ D^-$ case, backgrounds (3–5) are estimated using the data and only the uncertainty in the scaling factor for the subtracted distributions is taken into account. A second source of systematic error comes from the uncertainties in track and photon reconstruction efficiencies, which are 1% per track, 1.5% per photon and 5% per $K_S^0$, respectively. The systematic error ascribed to the cross section calculation is estimated to be 5% and includes the error on the differential ISR luminosity and the error from the efficiency fit. Other contributions come from the uncertainty in the identifica-
tion efficiency and the absolute $D^0$ and $D^+$ branching fractions [20]. The total systematic uncertainties are 10% and comparable to the statistical errors in the differential cross section around the $\psi(3770)$ peak; for the other $M_{D^0}$ ranges statistical errors dominate.

In summary, we report measurements of $e^+ e^- \rightarrow D^0 \bar{D}^0$ and $e^+ e^- \rightarrow D^+ D^-$ exclusive cross sections for $\sqrt{s}$ near the $D^0 \bar{D}^0$ and $D^+ D^-$ thresholds with initial-state radiation. The observed $e^+ e^- \rightarrow D \bar{D}$ exclusive cross sections are consistent with recent BABAR measurements [21] and are in qualitative agreement with the coupled-channel model predictions of Ref. [22]. This includes the peak at 3.9 GeV/$c^2$ that is seen both in Belle and BABAR cross section spectra.

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[16] Charge-conjugate modes are included throughout this paper.